

# CP violation and related issues 

Part 3+4: Experiments

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## Contents

Principle of measurement
Experimental considerations
Choice of boost
Spectrometer design
Babar and Belle spectrometers

## Principle of measurement

Principle of measurement：
－Produce pairs of $B$ mesons，moving in the lab system
－Find events with $B$ meson decay of a certain type（usually $B->f_{C P}-$ CP eigenstate）
－Measure time difference between this decay and the decay of the associated $B$（ $f_{\text {tag }}$ ）（from the flight path difference）
－Determine the flavour of the associated $B$（ $B$ or anti－B）
－Measure the asymmetry in time evolution for $B$ and anti－B

Restrict for the time being to $B$ meson production at $Y(4 s)$

##  <br> $B$ meson production at $Y(4 s)$




## Experimental considerations

What kind of vertex resolution do we need to measure the asymmetry?

$$
P\left(B^{0}\left(\bar{B}^{0}\right) \rightarrow f_{C P}, t\right)=e^{-\Gamma t}\left(1 \mp \sin \left(2 \phi_{1}\right) \sin (\Delta m t)\right)
$$



Want to distiguish the decay rate of $B$ (dotted) from the decay rate of anti-B (full).
-> the two curves should not be smeared too much

Integrals are equal, time information mandatory! (at $\mathrm{Y}(4 \mathrm{~s})$, but not for incoherent production)

May 17-25, 2005 Course at University of Barcelona Peter Križan, Ljubljana

## Experimental considerations

B decay rate vs $t$ for different as vertex resolutions in units of typical B flight length $\sigma(\mathrm{z}) / \beta \gamma \tau \mathrm{C}$


## Experimental considerations

Since there are no pure samples of $B$ and $B$ tags, what is really measured is the probability that the tagging $B$ is a $B$ or a anti- $B$.
Denote with x : variable between $-1(\operatorname{tag}=a n t i-B)$ and $+1(\operatorname{tag}=\mathrm{B})$ and the probability that the tag is wrong with $w(x)$
Probability density function for an event with $t$ and $x$ is

$$
f(t, x, A) d x d t=e^{-\Gamma t}[1+q(x) A \sin \Delta m t] n(x) d x d t
$$

with $A=C P$ asymmetry (e.g. $\sin 2 \phi_{1}$ ), $q(x)=1-2 w$
Taking into account the finite vertex resolution, we arrive at
$f\left(t, x, A, \sigma_{t}\right) d x d t=\left[\int \frac{1}{\sqrt{2 \pi \sigma_{t}}} e^{-\frac{1}{2}\left(\frac{1-t^{\prime}}{\sigma_{t}}\right)^{2}} e^{-\Gamma\left|\ell^{\prime}\right|}\left[1+q(x) A \sin \Delta m t^{\prime}\right] n(x) d t^{\prime}\right] d x d t$

## Experimental considerations

This can be rewritten as

$$
\begin{gathered}
f(t, x, A, \sigma) d x d t=[E(t)+A q(x) S(t)] n(x) d x d t \\
E(t)=\int \frac{1}{\sqrt{2 \pi \sigma_{t}}} e^{-\frac{1}{2}\left(\frac{t-t^{\prime}}{\sigma_{t}}\right)^{2}} e^{-\Gamma\left|t^{\prime}\right|} d t^{\prime}, \\
S(t)=\int \frac{1}{\sqrt{2 \pi \sigma_{t}}} e^{-\frac{1}{2}\left(\frac{t-t^{\prime}}{\sigma_{t}}\right)^{2}} e^{-\Gamma\left|t^{\prime}\right|} \sin \Delta m t^{\prime} d t^{\prime} .
\end{gathered}
$$

## Experimental considerations

The log-likelihood function is a sum over all reconstructed and tagged events

$$
\begin{aligned}
& \ln \mathcal{L}=\ln \prod_{i=1}^{N} f\left(t_{i}, x_{i}, A, \sigma_{t}\right)=\sum_{i=1}^{N} \ln f\left(t_{i}, x_{i}, A, \sigma_{t}\right) \\
& \ln \prod_{i=1}^{N} f\left(t_{i}, x_{i}, A, \sigma_{t}\right)=\sum_{i=1}^{N} \ln [(1+A q(x) S(t) / E(t)) E(t) n(x)] \\
&=\sum_{i=1}^{N} \ln (1+A q(x) S(t) / E(t))+C \\
& \longmapsto \ln \mathcal{L}^{\prime}=\sum_{i=1}^{N} \ln \left(1+A \frac{q S}{E}\right)
\end{aligned}
$$

## Experimental considerations

Error on the asymmetry
parameter A can be evaluated

$$
\quad \frac{1}{\sigma_{A}^{2}}=N \int_{-1}^{1} \int_{-\infty}^{\infty} \frac{1}{f}\left(\frac{\partial f}{\partial A}\right)^{2} n(x) d t d x
$$

$$
\sigma_{A} \approx \frac{\sigma_{0}}{\sqrt{N} \sqrt{\left\langle q^{2}\right\rangle}}, \quad \quad \text { Use } \mathrm{f}\left(\mathrm{t}, \mathrm{x}, \mathrm{~A}, \sigma_{\mathrm{t}}\right) \text { to get } \sigma_{\mathrm{A}}
$$

$$
\left\langle q^{2}\right\rangle \equiv \int_{-1}^{1} q^{2}(x) n(x) d x
$$

$$
\sigma_{0} \equiv \frac{1}{\sqrt{\int_{-\infty}^{\infty} \frac{\left(\frac{S(t)}{E(t)}\right)^{2}}{\left[1+A \frac{S(t)}{E(t)}\right]} E(t) d t}}
$$

## Experimental considerations

Final expression for the asymmetry error (error on $\sin 2 \phi_{1}$ ) as a function of vertex resolution and wrong tag probability
$\sigma_{A}\left(A, \Delta m / \Gamma, \sigma_{t}, N, w\right)=\frac{\sigma_{0}\left(A, \Delta m / \Gamma, \sigma_{t}\right)}{\sqrt{N} \sqrt{\epsilon}(1-2 w)}$
N : number of reconstructed events,
$\varepsilon$ : tagging efficiency
w: wrong tag probability

## Experimental considerations

Error on $\sin 2 \phi_{1}=\sin 2 \beta$ as function of vertex resolution in units of typical B flight length $\sigma(z) / \beta \gamma \tau \mathrm{C}$

For 1 event

for 1000 events


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## Experimental considerations

Choice of boost $\beta \gamma$ :
Vertex resolution vs. path length
Typical B flight length: $z_{B}=\beta \gamma \tau C$
Typical two-body topology: decay products at $90^{\circ}$ in cms; at $\theta=\operatorname{atan}(1 / \beta \gamma)$ in the lab
Assume: vertex resolution determined by multiple scattering in the first detector layer and beam pipe wall at $r_{0}$


$$
\begin{aligned}
& \sigma_{\theta}=15 \mathrm{MeV} / \mathrm{p} \sqrt{ }\left(\mathrm{~d} / \sin \theta \mathrm{X}_{0}\right) \\
& \sigma(\mathrm{z})=\mathrm{r}_{0} \sigma_{\theta} / \sin ^{2} \theta \\
& \Rightarrow \sigma(\mathrm{z}) \alpha r_{0} / \sin ^{5 / 2} \theta
\end{aligned}
$$

## Experimental considerations

Choice of boost $\beta \gamma$ :
Vertex resolution in units of typical B flight length

Boost around $\beta \gamma=0.8$ seems optimal

However....
$\beta \gamma \tau C / \sigma(z)$


## Experimental considerations

Which boost...
Arguments for a smaller boost:

- Larger boost -> smaller acceptance ->
- Larger boost -> it becomes hard to damp the betatron oscillations of the low energy beam: less synchrotron radiation at fixed ring radius (same as the high energy beam)


Figure 4. The acceptance of a detector covering $\left|\cos \theta_{l a b}\right|<0.95$ for five uncorrelated particles as a function of the energy of the more energetic beam in an asymmetric collider at the $\Upsilon(4 \mathrm{~S})$.

## Experimental considerations

Detector form: symmetric for symmetric energy beams; extended in the boost direction for an asymmetric collider.


How many events?

Rough estimate:
Need $\sim 1000$ reconstructed B-> J/ $\psi \mathrm{K}_{\mathrm{S}}$ decays with J/ $\psi$-> ee or $\mu \mu$, and $\mathrm{K}_{s^{-}}>\pi^{+} \pi^{-}$
$1 / 2$ of $Y(4 s)$ decays are $B^{0}$ anti- $B^{0}$ (but 2 per decay)
$\mathrm{BR}\left(\mathrm{B}->\mathrm{J} / \psi \mathrm{K}^{0}\right)=8.410^{-4}$
$\operatorname{BR}(\mathrm{J} / \psi->$ ee or $\mu \mu)=11.8 \%$
$1 / 2$ of $K^{0}$ are $K_{S}, B R\left(K_{S^{-}}->\pi^{+} \pi^{-}\right)=69 \%$
Reconstruction effiency ~ 0.2 (signal side: 4 tracks, vertex, tag side pid and vertex)

$$
\begin{aligned}
N(Y(4 s)) & =1000 /\left(1 / 2 * \frac{1}{2} * 2 * 8.410^{-4} * 0.118 * 0.69 * 0.2\right)= \\
& =140 \mathrm{M}
\end{aligned}
$$

## How to produce 140 M BB pairs?

Want to produce 140 M pairs in two years
Assume effective time available for running is $10^{7} \mathrm{~s}$ per year.
-> need a rate of $14010^{6}$ / (2 $10^{7} \mathrm{~s}$ ) $=7 \mathrm{~Hz}$
Observed rate of events $=$ Cross section $\times$ Luminosity

$$
\frac{d N}{d t}=L \sigma
$$

Cross section for $\mathrm{Y}(4 \mathrm{~s})$ production: $1.1 \mathrm{nb}=1.110^{-33} \mathrm{~cm}^{2}$
-> Accelerator figure of merit luminosity has to be

$$
L=6.5 / \mathrm{nb} / \mathrm{s}=6.510^{33} \mathrm{~cm}^{-2} \mathrm{~s}^{-1}
$$

This is much more than any other any other accelerator achieved before!


## Colliders: asymmetric B factories




Accelerator performace

Observed rate of events $=$ Cross section $\times$ Luminosity

$$
\frac{d N}{d t}=L \sigma
$$

Accelerator figures of merit: luminosity $L$
and integrated luminosity

$$
L_{\mathrm{int}}=\int L(t) d t
$$

Records:

$$
\begin{aligned}
& \mathrm{L}_{\text {peak }}=15.81 / \mathrm{nb} / \mathrm{sec}(\text { May } 18,2005)\left(=1.58 \times 10^{34} \mathrm{~s}^{-1} \mathrm{~cm}^{-2}\right) \\
& \mathrm{L}_{\text {int }}=434.355 / \mathrm{fb}(\text { May. 18, 2005 }) \\
& \sim 470 \text { М вв pairs }
\end{aligned}
$$







## Flavour tagging

Was it a B or anti- B that decayed to the CP eigenstate?

Look at the decay products of the associated $B$

- Charge of high momentum lepton


Flavour tagging

Was it a B or anti-B that decayed to the CP eigenstate?
Look at the decay products of the associated B

- Charge of high momentum lepton
- Charge of kaon
- Charge of 'slow pion' (from $D^{*}->D \pi$ decay)
- .....

Charge measured from curvature in magnetic field, need reliable particle identification




## Requirement: measure both



## $b->c$ anti-c s CP=+1 and CP=-1 eigenstates

$$
a_{f_{C P}}=-\operatorname{Im}\left(\lambda_{f_{C P}}\right) \sin (\Delta m t)
$$

Asymmetry sign depends on the CP parity of the final state $f_{\text {CP, }} \eta_{\text {fcp }}=+-1$

$$
\lambda_{f_{C P}}=\eta_{f_{C P}} \frac{q}{p} \frac{\bar{A}_{\bar{f}_{C P}}}{A_{f_{C P}}}
$$

$\mathrm{J} / \psi \mathrm{K}_{\mathrm{S}}\left(\pi^{+} \pi^{-}\right): \mathrm{CP}=-1$
$\bullet \mathrm{J} / \psi: \mathrm{P}=-1, \mathrm{C}=-1$ (vector particle $\mathrm{JPC}^{\mathrm{P}}=1^{--}$): $\mathrm{CP}=+1$
$\bullet K_{S}\left(->\pi^{+} \pi^{-}\right): C P=+1$, orbital ang. momentum of pions=0 ->

$$
\mathrm{P}\left(\pi^{+} \pi^{-}\right)=\left(\pi^{-} \pi^{+}\right), \mathrm{C}\left(\pi^{-} \pi^{+}\right)=\left(\pi^{+} \pi^{-}\right)
$$

$\bullet$-rbital ang. momentum between $\mathrm{J} / \psi$ and $\mathrm{K}_{\mathrm{S}} \mathrm{I}=1, \mathrm{P}=(-1)^{1}=-1$
$\mathrm{J} / \psi \mathrm{K}_{\mathrm{L}}(3 \pi)$ : $\mathrm{CP}=+1$
Opposite parity to $\mathrm{J} / \psi \mathrm{K}_{\mathrm{S}}\left(\pi^{+} \pi^{-}\right)$, because $\mathrm{K}_{\mathrm{L}}(3 \pi)$ has $\mathrm{CP}=-1$ -> need $\mathrm{K}_{\mathrm{L}}$ detection



Tracking: Belle central drift chamber
-50 layers of wires ( 8400 cells) in 1.5 Tesla magnetic field
-Helium:Ethane 50:50 gas, Al field wires, CF inner wall with cathodes, and preamp only on endplates
-Particle identification from ionization loss (5.6-7\% resolution)



## Identification

Hadrons（ $\pi, \mathrm{K}, \mathrm{p}$ ）：
－Time－of－flight（TOF）
－ $\mathrm{dE} / \mathrm{dx}$ in a large drift chamber
－Cherenkov counters

Electrons：electromagnetic calorimeter

Muon：muon chambers in the instrumented magnet yoke

## Identification with $\mathrm{dE} / \mathrm{dx}$ measurement

$\mathrm{dE} / \mathrm{dx}$ performance in a large drift chamber.

Essential for hadron identification at low momenta.


## Cherenkov counters

Essential part of particle identification systems.
Cherenkov relation: $\boldsymbol{\operatorname { c o s }} \theta=\mathbf{c} / \mathbf{n v}=\mathbf{1} / \beta \mathbf{n}$

Threshold counters --> count photons to separate particles below and above threshold; for $\beta<\beta_{\mathrm{t}}=1 / \mathrm{n}$ (below threshold) no Cerenkov light is emitted

Ring Imaging (RICH) --> measure Čerenkov angle and count photons



Use Cherenkov relation $\cos \theta=c / n v=1 / \beta n$ to determine velocity from angle of emission

DIRC: a special kind of RICH (Ring Imaging Cherenkov counter) where Čerenkov photons trapped in a solid radiator (e.q. quartz) are propagated along the radiator bar to the side, and detected as they exit and traverse a gap.


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Babar DIRC: a Bhabha event $\mathrm{e}^{+} \mathrm{e}^{-}-->\mathrm{e}^{+} \mathrm{e}^{-}$




To check the performance, use kinematically selected decays:
$D^{*+}->\pi^{+} D^{0}, D^{0}->K^{-} \pi^{+}$



## Calorimetry Design

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IITITIII

## Requirements

-Best possible energy and position resolution: 11 photons per $\mathrm{Y}(4 \mathrm{~S})$ event; 50\% below 200 MeV in energy
-Acceptance down to lowest possible energies and over large solid angle
-Electron identification down to low momentum

## Constraints

-Cost of raw materials and growth of crystals

- Operation inside magnetic field
-Background sensitivity


## Implementation

Thallium-doped Cesium-Iodide crystals with 2 photodiodes per crystal Thin structural cage to minimize material between and in front of crystals


## Muon and $\mathrm{K}_{\mathrm{L}}$ detector

Up to 21 layers of resistiveplate chambers (RPCs) between iron plates of flux return

Muon identification >800 $\mathrm{MeV} / \mathrm{c}$
Neutral hadrons $\left(\mathrm{K}_{\mathrm{L}}\right)$ detection - also with electromagnetic calorimeter

Bakelite RPCs at BABAR
Glass RPCs at Belle

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